



# Evolutionary lessons for wind energy efficiency

also known as  
**Optimizing the Turbine Placement  
of Large Wind Farms**

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Wall Street Journal (05/07/11) Miriam Jordan

Biology helps to optimise wind farms · News in Science (ABC Science)

http://www.abc.net.au/science/articles/2011/05/05/30110504091842.htm

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### Biology helps to optimise wind farms

Anna Salleh  
ABC

Thursday, 5 May 2011

Evolutionary algorithms are being used to work out the best placement of wind turbines to maximise their energy output.



Wind turbines can block the flow of wind to other turbines, depending on where they are placed (Source: Chromatika Multimedia/iStockphoto)

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**Evolutionary lessons for wind farm efficiency** 

5 May 2011 ... Evolution is providing the inspiration for computer science research in Australia to find the best placement of turbines to increase wind ...

[www.sciencedaily.com/releases/2011/05/110504091842.htm](http://www.sciencedaily.com/releases/2011/05/110504091842.htm) - Cached

# Motivation

## Renewable Energy:

- .....→ Has gained increasing interest
- .....→ Is clean
- .....→ Substantial to decrease CO<sub>2</sub> emission
- .....→ Is a huge market
- .....→ Large developing effort
- .....→ Has many challenging questions.

## Wind Energy:

- .....→ Major player in renewable energy
- .....→ Since 2005 the cumulative installed capacity of wind energy within the EU has almost doubled (from 40000 MW to 74000 MW).
- .....→ In 2009, 39% of all new energy capacity installed in the EU was based on wind.
- .....→ Roughly 8800 wind turbines in Europe which helped to save 180 Mio tons of CO<sub>2</sub> since the beginning of 2009.

## Largest Wind Farms:

- .....→ Roscoe Wind Farm (Texas, 627 turbines, 781 MW)
- .....→ Vlorë Wind Farm (Albania, 250 turbines, 500 MW)

## Recent News:

- .....→ Thanet Wind Farm (Offshore (UK), 100 turbines, 300 MW)
- .....→ Ontario's 21,000 Megawatts Offshore Potential
- .....→ Google invests 38.8 Mio. USD in Wind Energy

## Very Recent News (9 May 2011):

“Special Report on Renewable Energy Sources and Climate Change Mitigation”

- .....→ Renewable energy could make up 77% in 2050
- .....→ Wind energy could be responsible for 20%



Source: Wind Power Ninja



# Wind Speed and Energy

## Wind Speed:

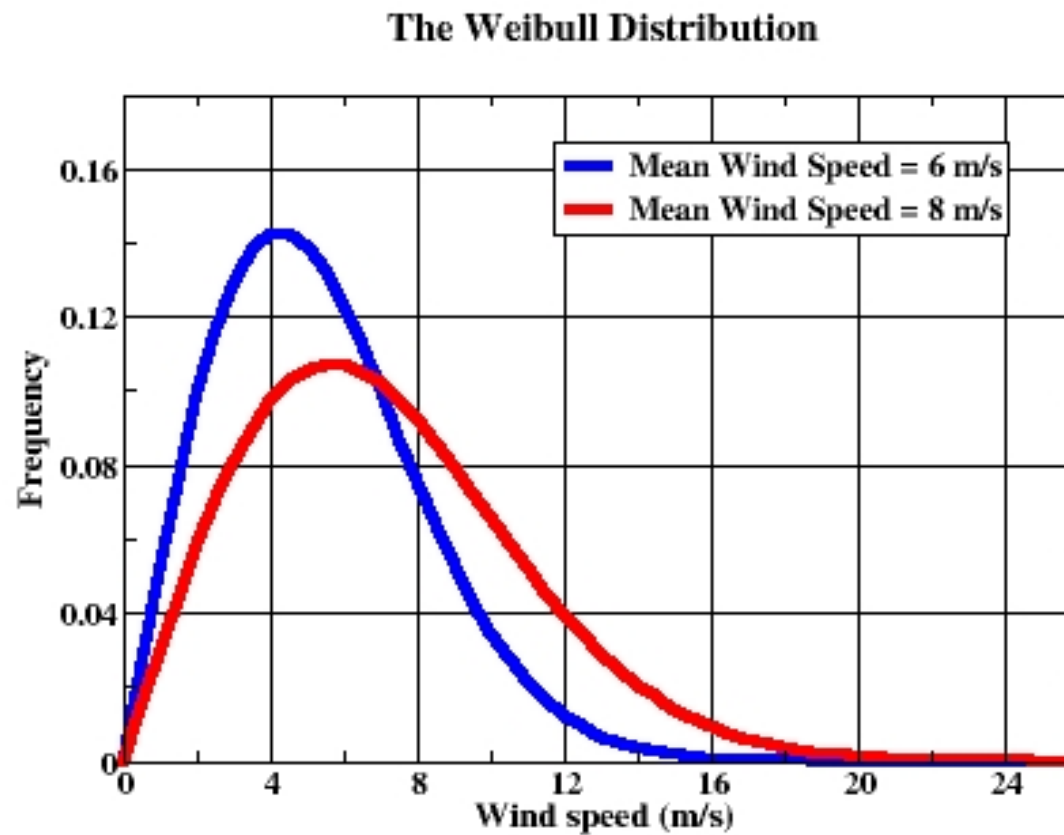
- .....→ Most crucial for energy production
- .....→ Varies over time
- .....→ Depends on seasonal effects
- .....→ Weibull distribution gives a good representation of the variation in hourly mean wind speed over a year at many typical sites

Probability density function:  $p(v, k, c) = k/c(v/c)^{k-1} e^{-(v/c)^k}$

k: Weibull shape parameter

c: Weibull scale parameter

## Example Weibull distribution:

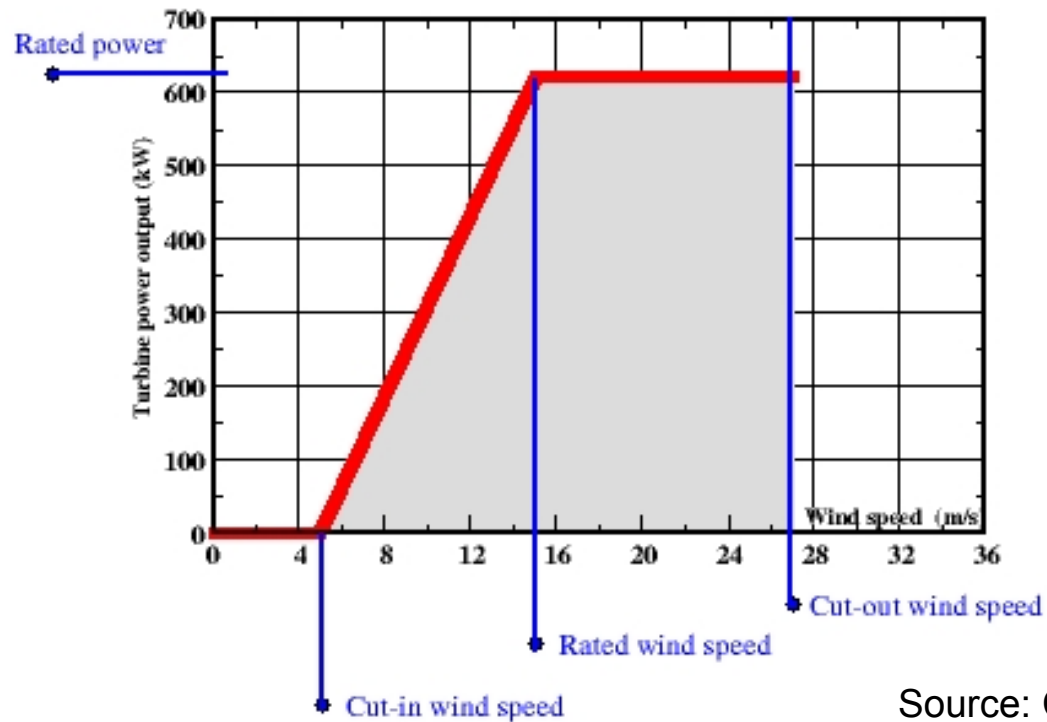


Source: Canadian Wind Energy Atlas

Assume linear energy function

$$\beta(v) = \begin{cases} 0 & v < v_{cut\_in} \\ \lambda v + \eta & v_{cut\_in} \leq v \leq v_{rated} \\ P_{rated} & v_{rated} < v < v_{cut\_out} \end{cases}$$

Idealized power curve for a wind turbine (example)



Source: Canadian Wind Energy Atlas

Expected energy output of turbine i:

$$P(\theta)$$

$$p_v(v(\theta), c(\theta), k(\theta))$$

$$E^i[\eta] = \int_{\theta} P(\theta) \int_v p_v(v(\theta), c(\theta), k(\theta)) \beta^i(v).$$

For wind farm with  
n turbines

$$E^{farm}[\eta] = \sum_{i=1}^n E^i[\eta]$$

?

What's wrong with that?

# Wake effects

## Wake Effect:

- .....→ On wind farms turbines are placed close to each other
- .....→ Energy capture of a turbine is influenced by the other turbines on the wind farm
- .....→ Turbines produce wake effects that reduce the wind speed usable for energy production
- .....→ Wake effects influence the efficiency of wind farms: turbines in the center may produce just 60% of the energy of turbines at the border, which leaves room for optimizations.

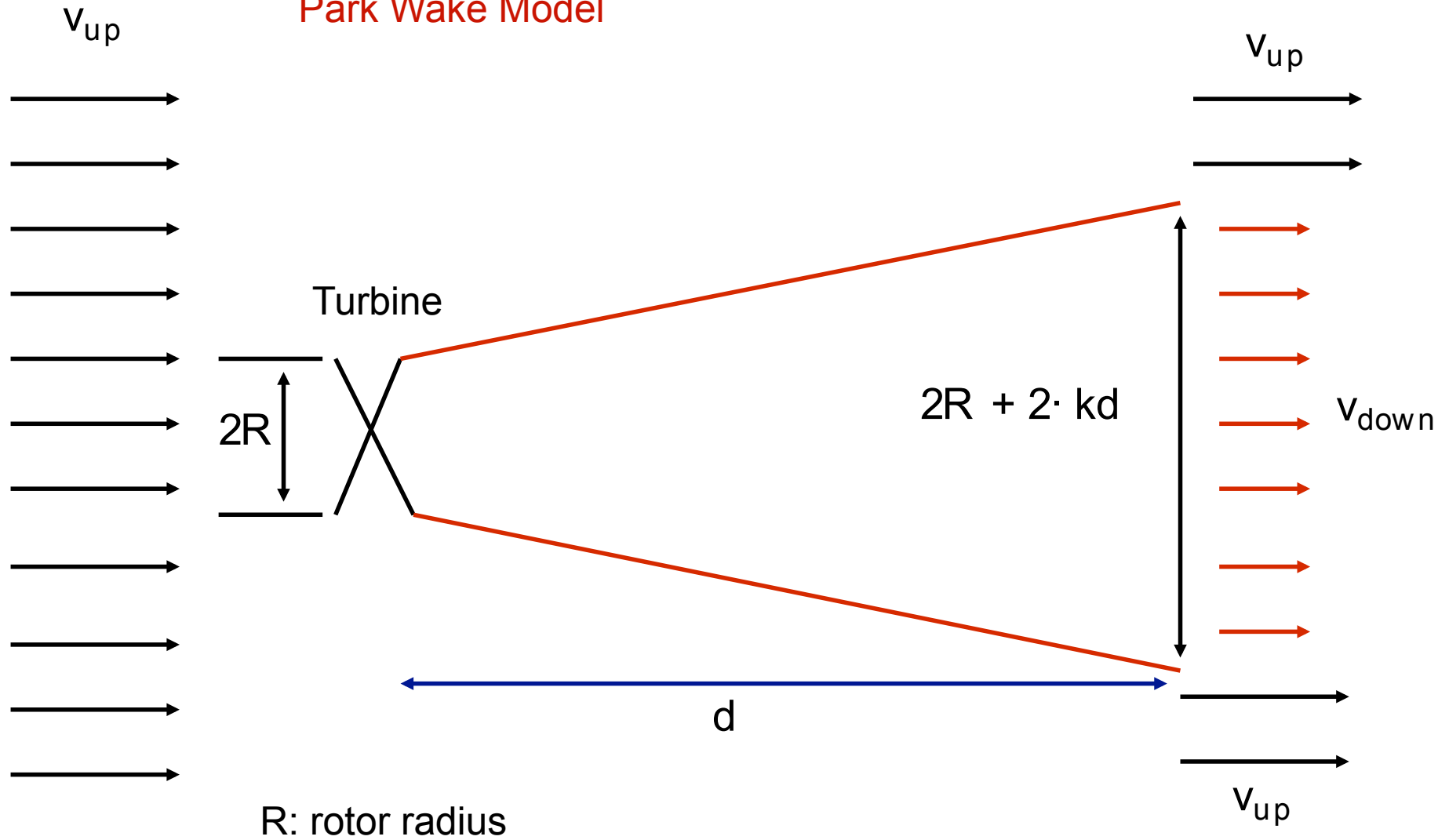
Wake



Source: Cooperative Institute for Research in Environmental Science

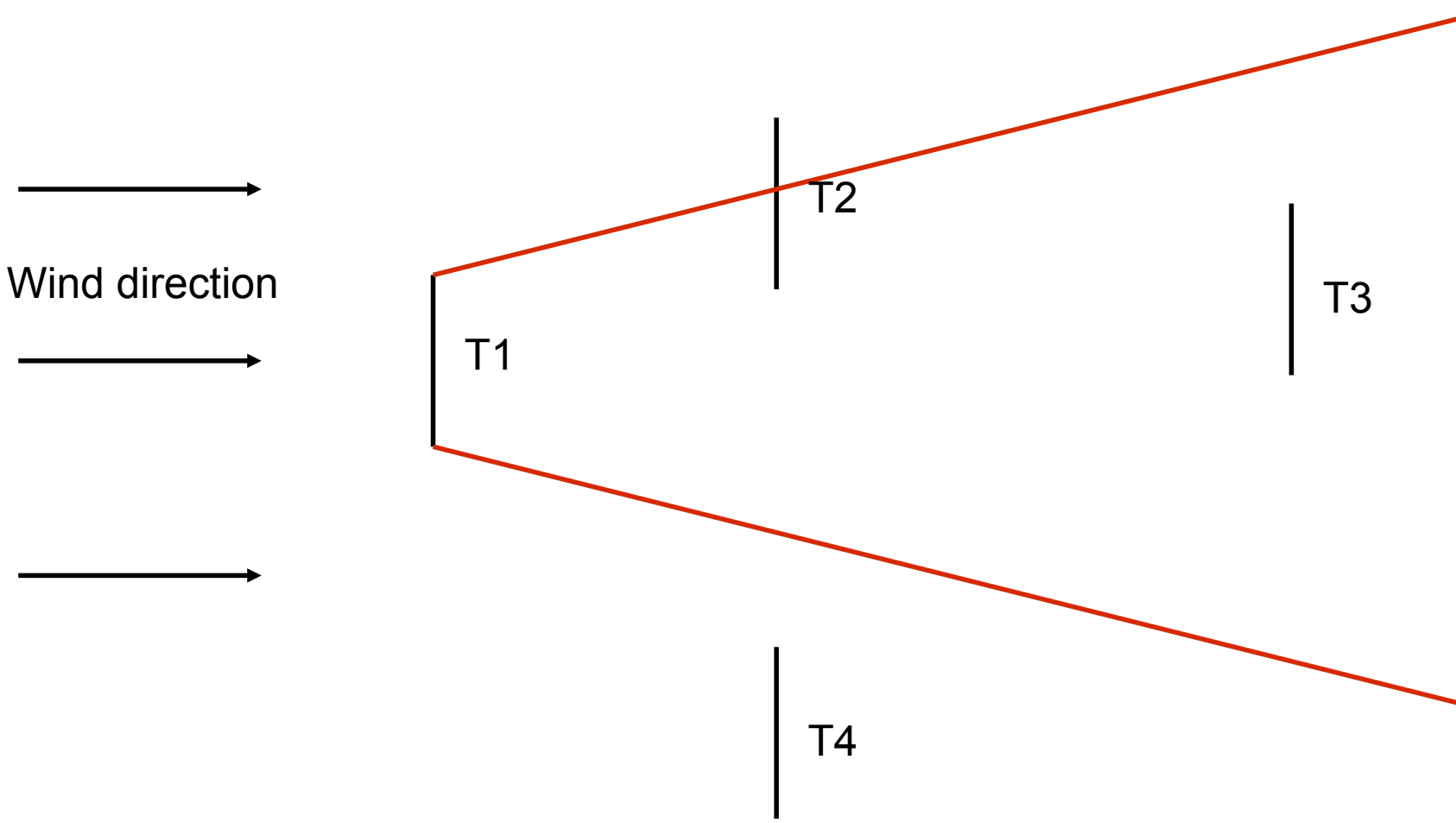


## Park Wake Model



R: rotor radius

# Wake effect



## Computation of the wake effect (Kusiak and Song 2010)

Let  $X = \{x_1, \dots, x_n\}$  and  $Y = \{y_1, \dots, y_n\}$  be x and y coordinates of the n turbines

**for**  $i = 1$  to number of turbines **do**

**for**  $\theta = 0^0$  to  $360^0$  **do**

**for**  $j = 1$  to  $n-1$  and  $j \neq i$  **do**

$$\delta_{i,j} = \cos^{-1} \left\{ \frac{o + R/\kappa}{\sqrt{(x_i - x_j + (R/\kappa)\cos\theta)^2 + (y_i - y_j + (R/\kappa)\sin\theta)^2}} \right\}$$

$$Vdef_{(i,j)} = u(\delta_{i,j} - \alpha) \frac{a}{(1 + b\delta_{i,j})^2}$$

**end for**

$$Vdef_i^\theta = \sqrt{\sum_j (Vdef_{(i,j)})^2}$$

$$c_i(\theta) = c_i(\theta) \times (1 - Vdef_i)$$

**end for**

**end for**

Wake effect only changes scaling parameter of Weibull distribution

Energy output of turbine  $i$  considering wake effect:

$$E^i [\eta] = \int_{\theta} P(\theta) \int_v p_v^{\theta}(v, c_i(\theta), k_i(\theta), x_i, y_i, X, Y) \beta^i(v)$$

Total energy output of the wind farm:

$$E^{farm} [\eta] = \sum_{i=1}^n E^i [\eta]$$

# Experimental Study

## Setting:

- .....→ Number of turbines:  $n$
- .....→ Positive coordinates:  $x_i$  and  $y_i$  for each turbine  $i$

## Constraints:

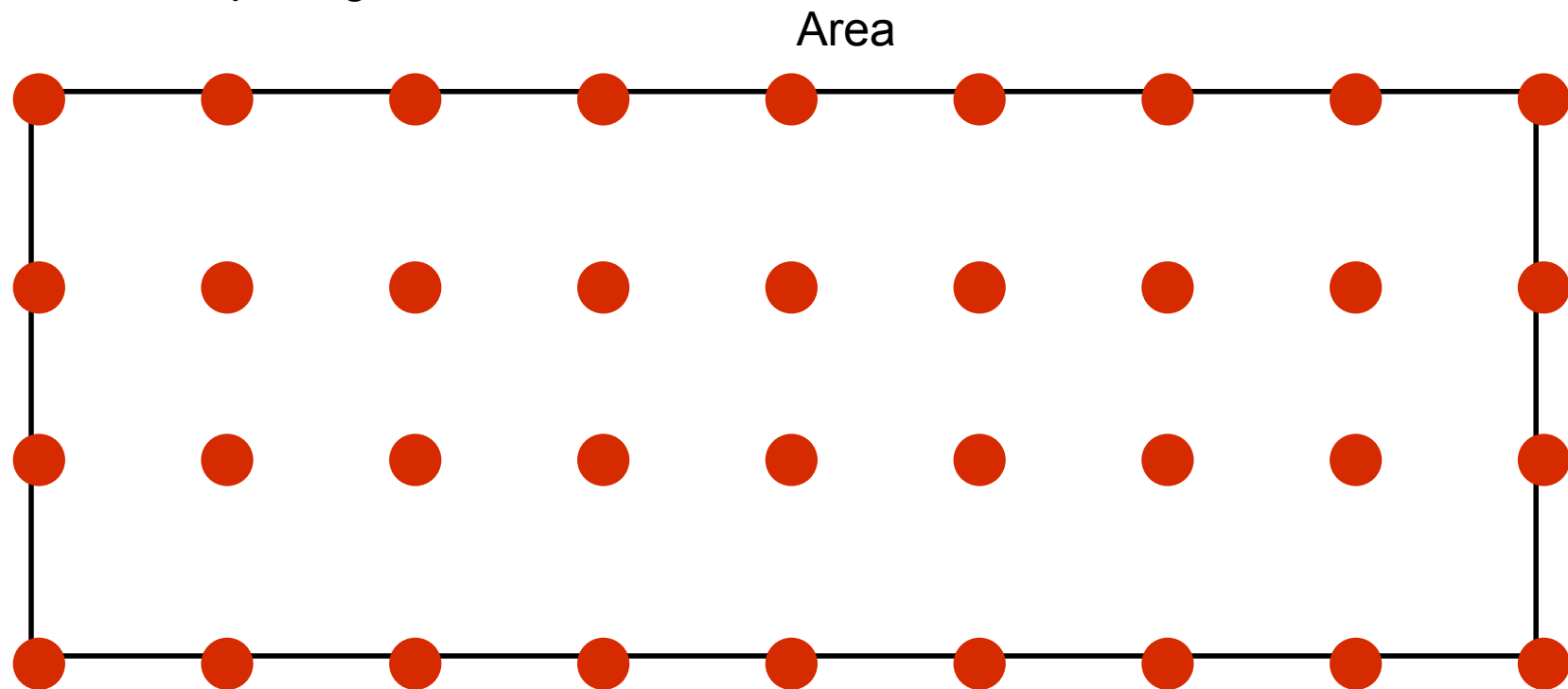
- .....→ Area and length  $l$  and wide  $w$ :  $\forall i : x_i \leq l \text{ and } y_i \leq w$
- .....→ Proximity constraints:  $\forall i, j, i \neq j : \sqrt{(x_i - x_j)^2 + (y_i - y_j)^2} \geq 8 \cdot R$

R: rotor radius

Area could include  $2n$  turbines

## Turbine Placement on wind farm

Maximal spacing initialization



## Wind Scenario (Kusiak and Song, Renewable Energy 2010)

$l-1$	$\theta^{l-1}$	$\theta^l$	$k$	$c$	$P(\theta)$	$l-1$	$\theta^{l-1}$	$\theta^l$	$k$	$c$	$P(\theta)$
0	0	15	2	7	0.0002	12	180	195	2	10	0.1839
1	15	30	2	5	0.008	13	195	210	2	8.5	0.1115
2	30	45	2	5	0.0227	14	210	225	2	8.5	0.0765
3	45	60	2	5	0.0242	15	225	240	2	6.5	0.008
4	60	75	2	5	0.0225	16	240	255	2	4.6	0.0051
5	75	90	2	4	0.0339	17	255	270	2	2.6	0.0019
6	90	105	2	5	0.0423	18	270	285	2	8	0.0012
7	105	120	2	6	0.029	19	285	300	2	5	0.001
8	120	135	2	7	0.0617	20	300	315	2	6.4	0.0017
9	135	150	2	7	0.0813	21	315	330	2	5.2	0.0031
10	150	165	2	8	0.0994	22	330	345	2.4	5	0.0097
11	165	180	2	9.5	0.1394	23	345	360	2	3.9	0.0317

Kusiak and Song use evolution strategy  
 Only results for up to 6 turbines.



## Experimental Studies:

- .....→ Use maximal spacing initialization for initial placement
- .....→ Improve by (10,20)-CMA-ES
- .....→ Include mechanism to deal with boundary constraints
- .....→ Improves results of Kusiak and Song
- .....→ **What results do we get for large wind farms?**

## Problem:

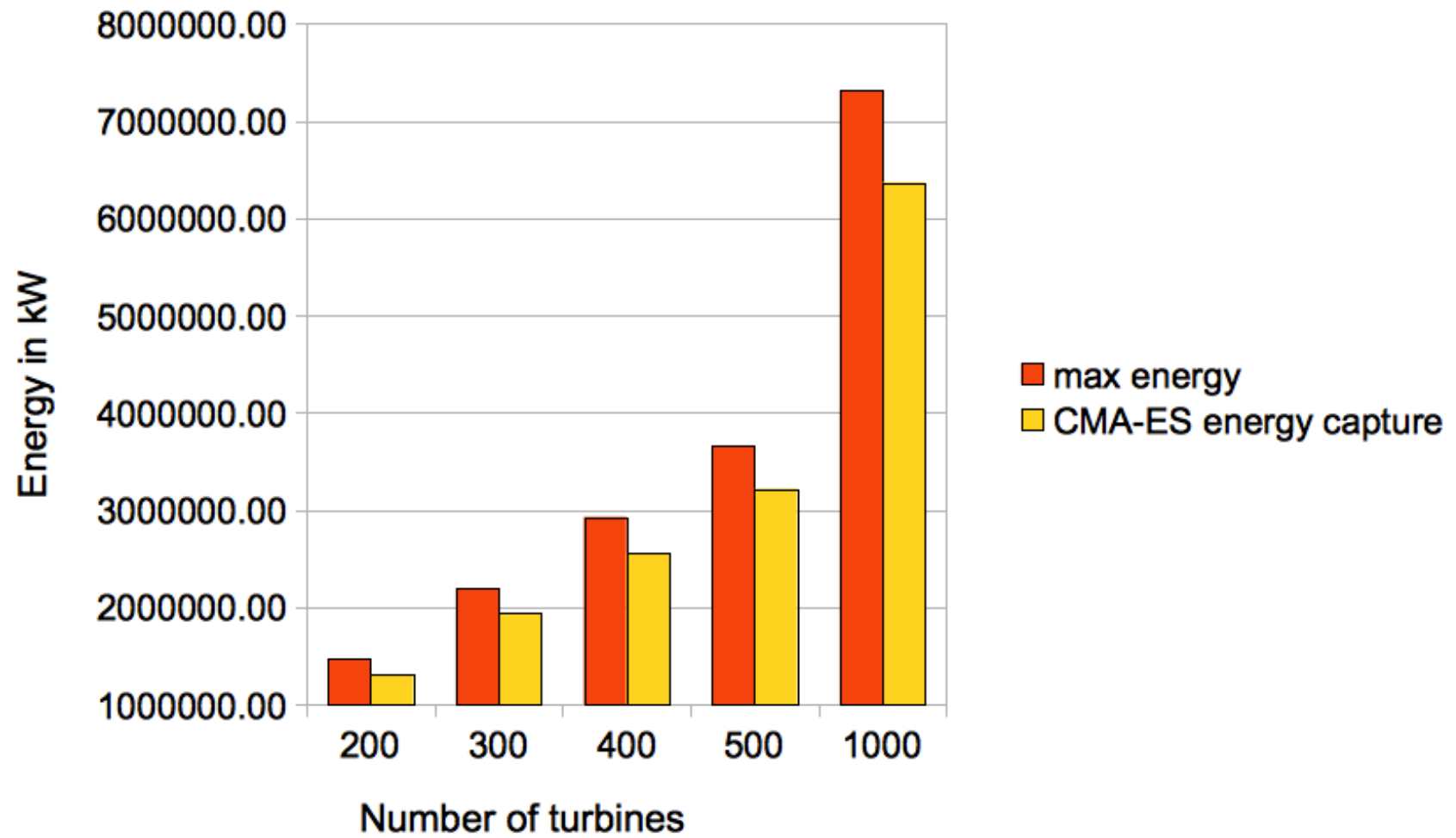
- .....→ Evaluation is very costly for large number of turbines
- .....→ Need sufficiently large number of generations (10000 or 20000) to get good results

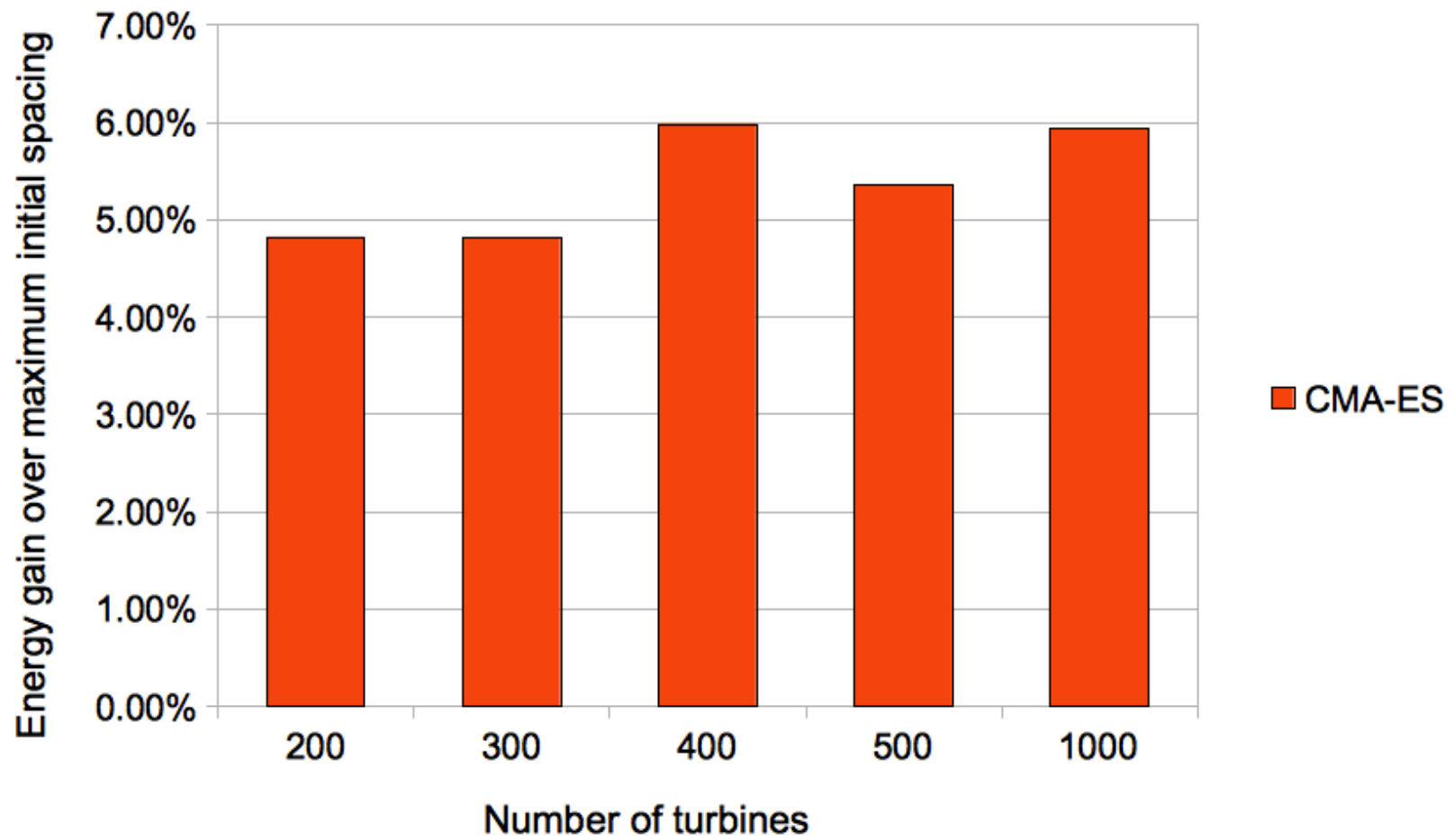
## Sequential Runtimes (predicted runtimes):

- .....→ 200 turbines: 1.4 sec (1 eval) => 2.8 days (10000 gen)
- .....→ 500 turbines: 8.2 sec (1 eval) => 11 days (10000 gen)
- .....→ 1000 turbines: 32.4 sec (1 eval) => 150 days (20000 gen)

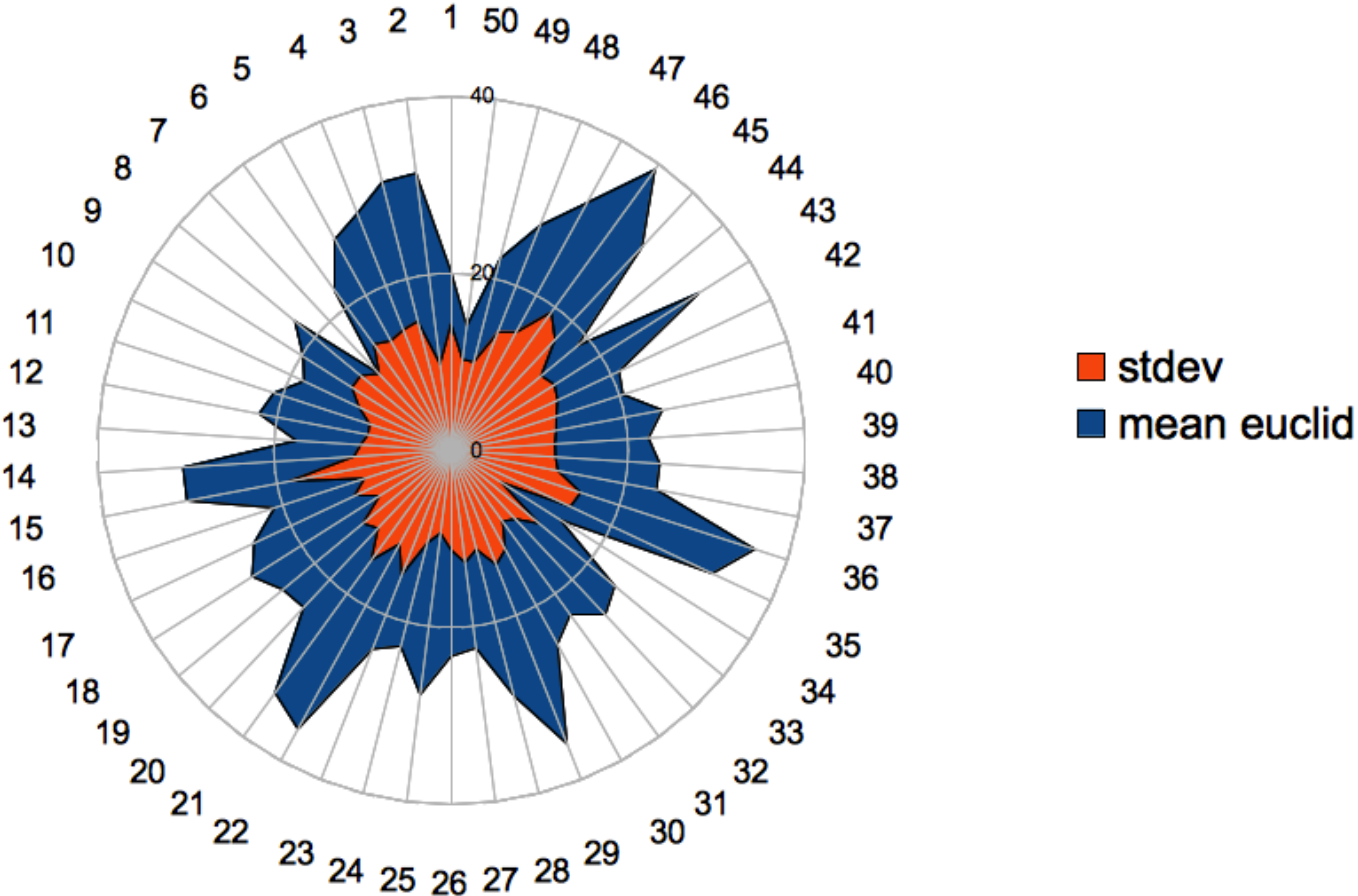
## Parallel Runtimes (cluster times per run):

- .....→ 200 turbines: 1.3 days (10000 generations, 30 runs)
- .....→ 500 turbines: 6 days (10000 generations, 30 runs)
- .....→ 1000 turbines: 12 days (20000 generations, 20 evaluations parallelized, 2 runs)





Euclidean distance moved by each turbine (data based on 30 runs)



Just 4,5 – 6%, so what?

1 year 7,2 ct per KWh, 1.5 MW turbines.

**200 turbines:**

.....→ 4.8 % of 1200 MW = 57.6 MW,

.....→ 504.576 MWh is **36.3 Mio USD/year**

**500 turbines:**

.....→ 5.4 % of 3.100 MW = 167.4 MW,

.....→ 1.466.424 MWh is **105.6 Mio USD/year**

**1000 turbines:**

.....→ 5.9 % of 6.000 MW = 354.0 MW,

.....→ 3.101.040 MWh is **223.3 Mio USD/year**

## Summary:

- .....→ Wind energy is an interesting field with challenging optimization problems
- .....→ Problems are very complex
- .....→ Evolutionary algorithms are well suited for tackling these problems
- .....→ Problems need parallelization of the algorithms
- .....→ There is a lot of money in this field (grants, government support, industry funding)
- .....→ **Computer Science should play a key role**

## Future Work:

- .....→ Nonlinear power curves
- .....→ Mixed wind farms
- .....→ More complex wake models
- .....→ Exploration of problem-specific algorithms
- .....→ Combination with other design parameters (cable length)
- .....→ Multi-objective problems
- .....→ Project at Future SOC Lab of the Hasso-Plattner-Institut (with Tobias Friedrich)

Thank you!