

# Maximising Axiomatization Coverage and Minimizing Regression Testing Time

# Who guards the guardians?

How to improve trust in **formal verification systems**?

$$a = b \vdash 2 = 1$$

Modern verification systems are large and complex systems

- Soundness bugs are not rare
- Such bugs are often hard to detect in a real proof

# “Auto-active” Verification Systems



Validating verification systems by

- Formal methods
- Code inspection
- **Testing**
- ...

# Program Language Semantics



Static checkers

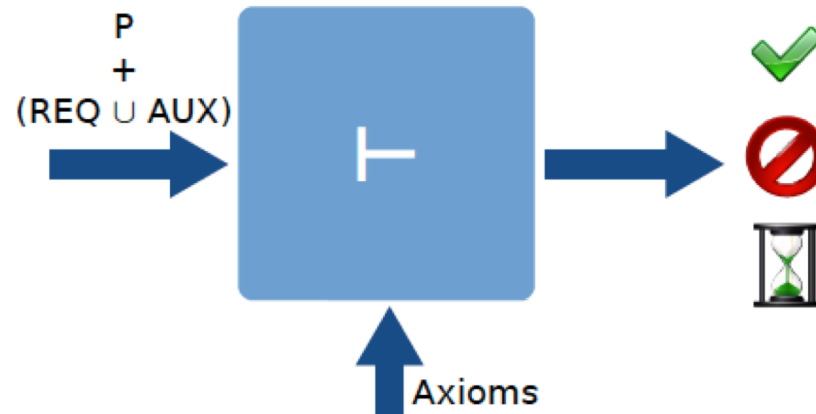
Verifying compilers

Logic frameworks

We have to test both!

But how to determine the quality of the test cases?

# Test Cases



A test case is a program  $P$ , together with requirement and auxiliary specifications.

Manually creating test cases is extremely time-consuming.

Computing coverage for the test cases takes from a few minutes to several hours.



# Case study: The KeY System

# The KeY System

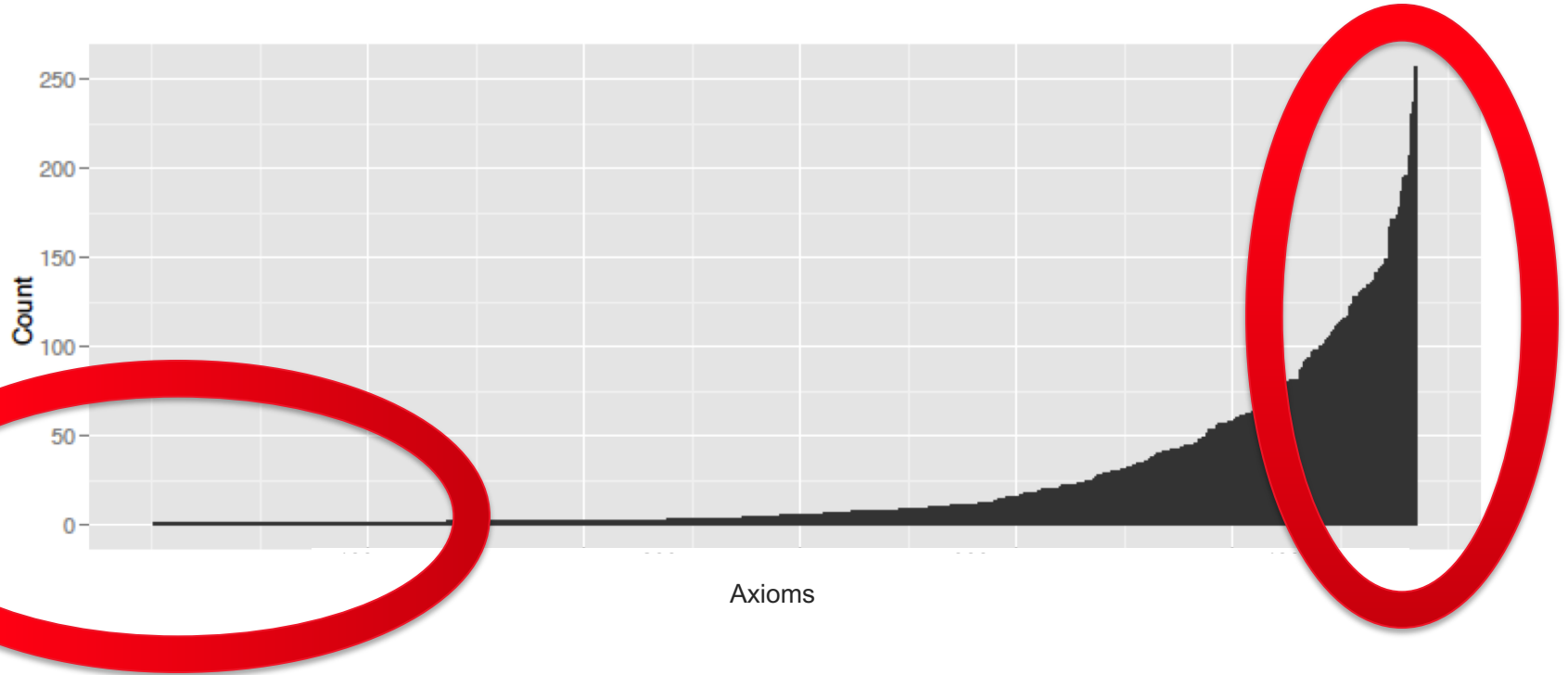
- Deductive verification system for JavaCard
- Sequent calculus for Java Dynamic Logic, uses symbolic execution for Java programs
- Interactive verification with automatic proof mode

## Important

- The semantics of JavaCard is encoded in 1520 axioms (“small, well-understood set of sentences”)

# Coverage Results (naïve, TAP 2013)

The 319 completeness tests of KeY covered 40% of all axioms (611 out of 1520).

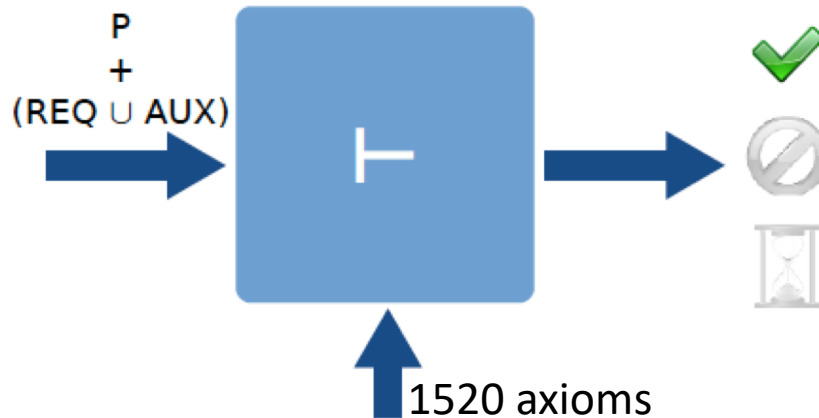




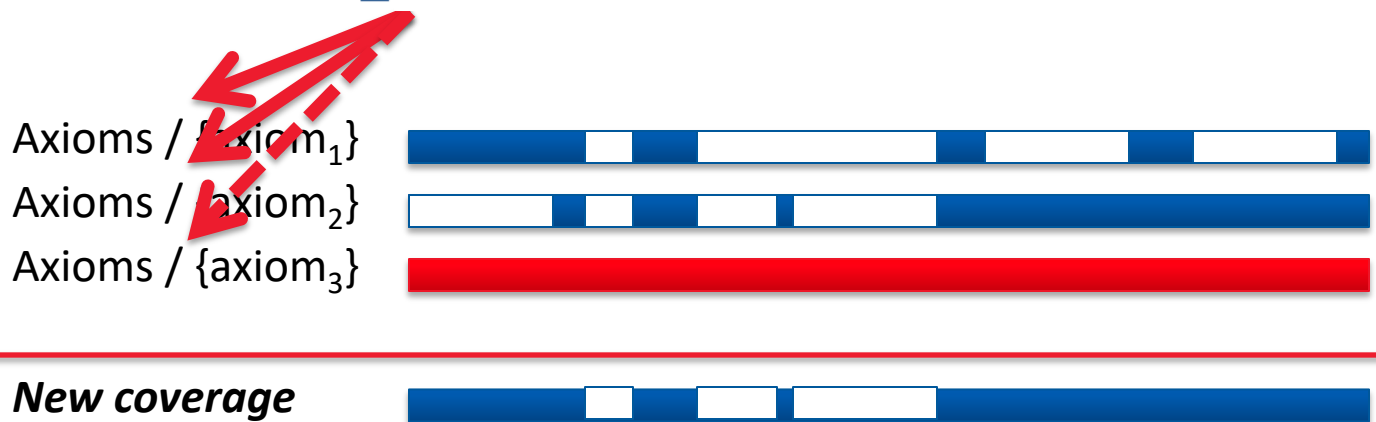
The background of the slide is a blue-tinted, halftone-style image of a university campus. In the foreground, several students are walking across a paved area. In the background, there are large, multi-story buildings with arched windows and a prominent tower with a clock face. The overall scene is a busy university environment.

# Heuristic Approaches

# Reusing Test Cases

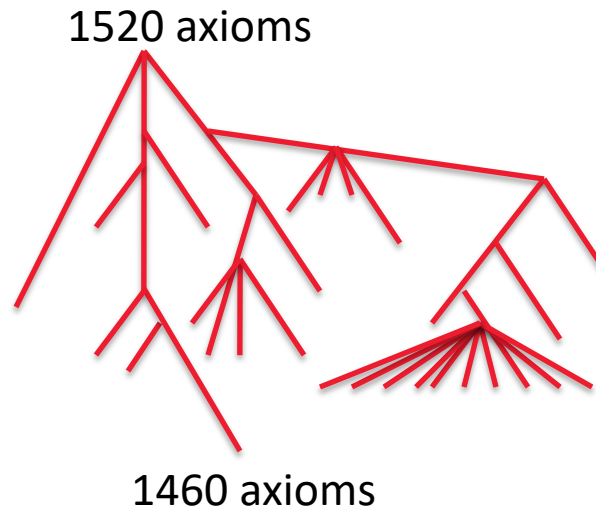


*drop one  
essential  
axiom*



Idea: given a test case  $T$ , run the tool with just a subset of the 1520 axioms.

# Reusing Test Cases



## Note:

- 24h per heuristic per test case
- Extremely fragile

Three simple heuristics to pick the “next axiom to drop”:

[0. Base case]

1. Depth-first

2. Depth-first, random

3. Greedy (try to

4. Breadth-first

5. Breadth-first, random selection

611 (40%)

703 (46%) Naive and good results

609 (40%) Base case

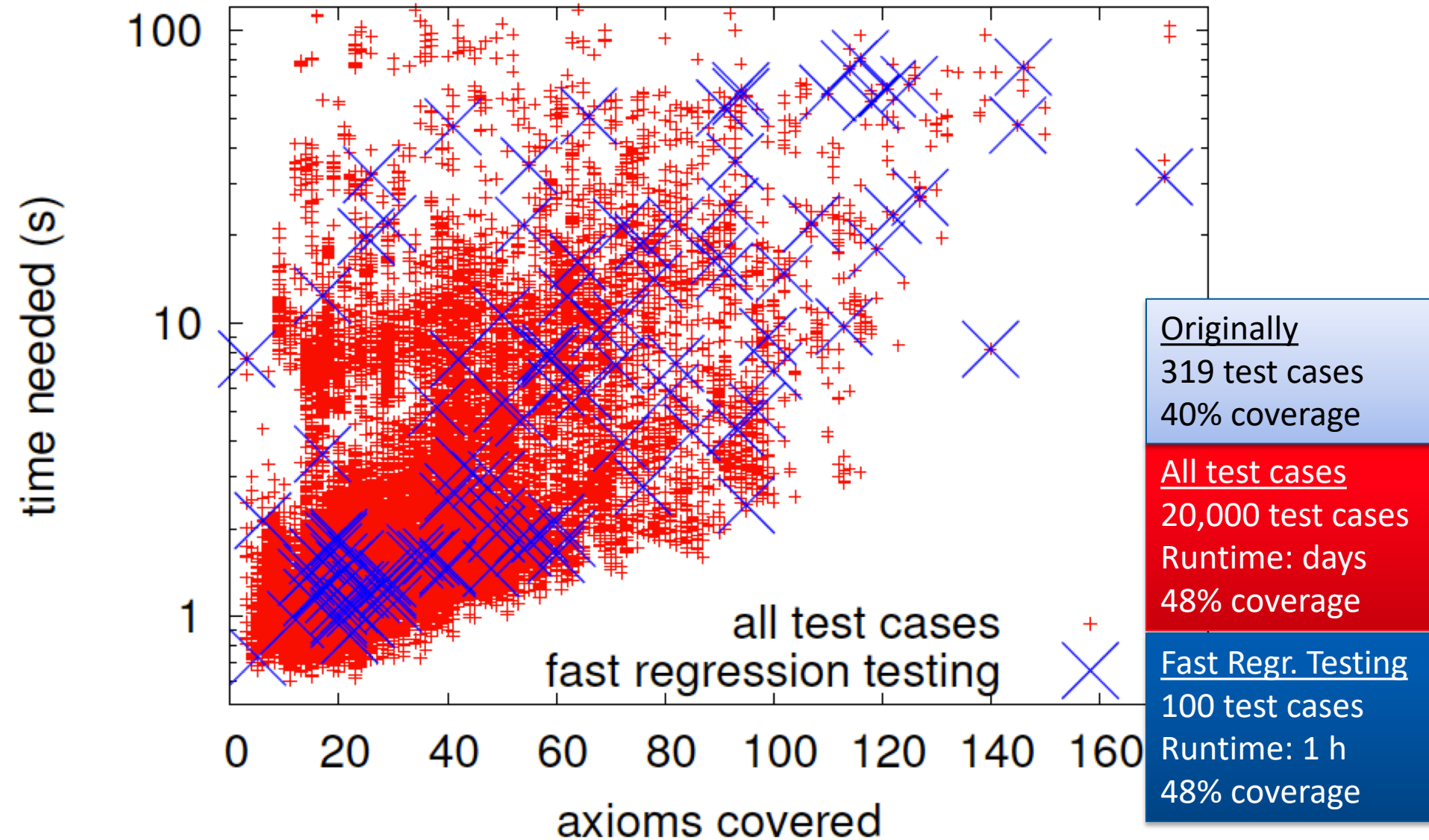
668 (44%) Greedy

687 (45%)

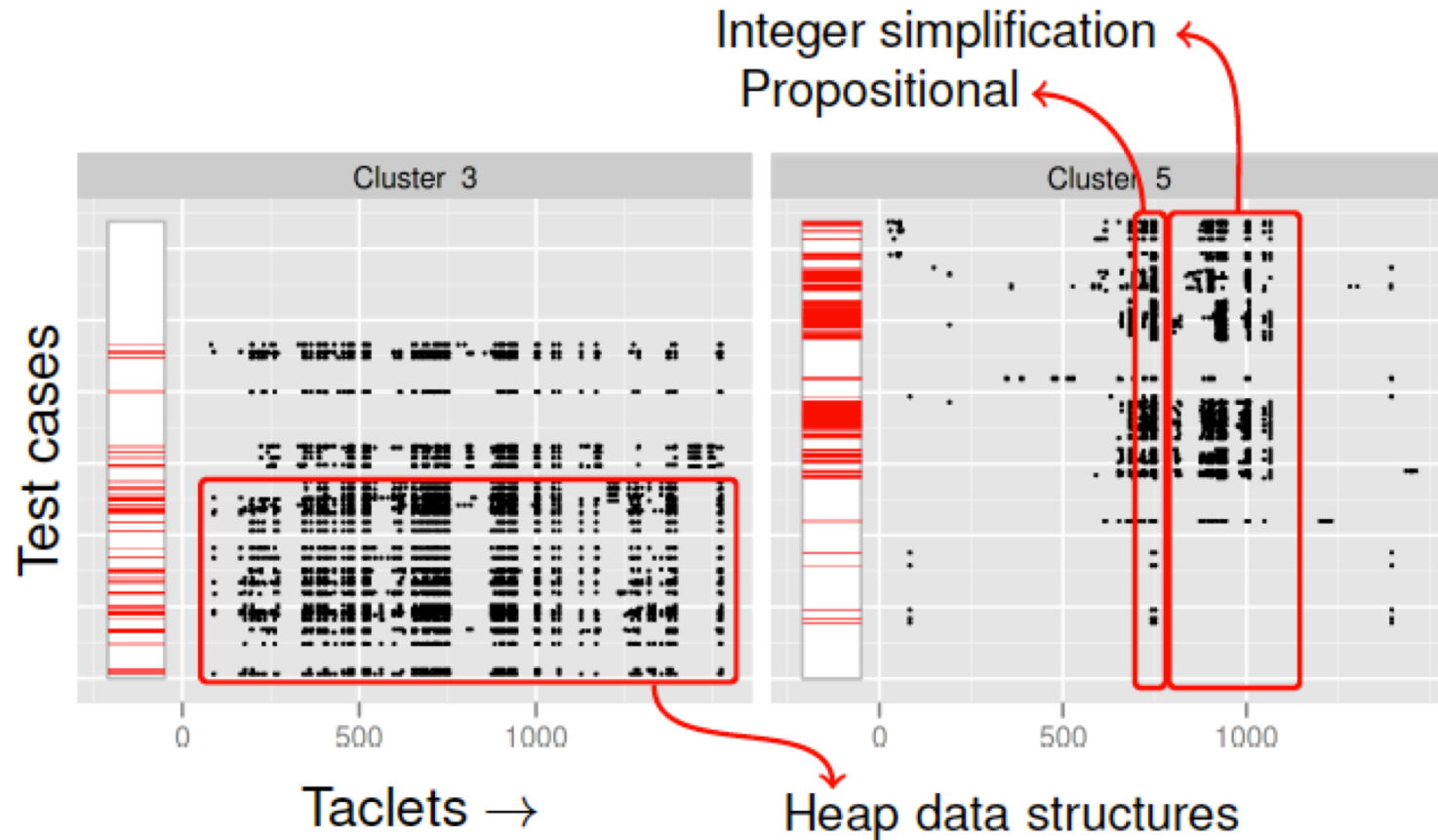
684 (45%)

→ Complimentary by design, verified by experiments.

# Maximising Coverage & Minimising Time



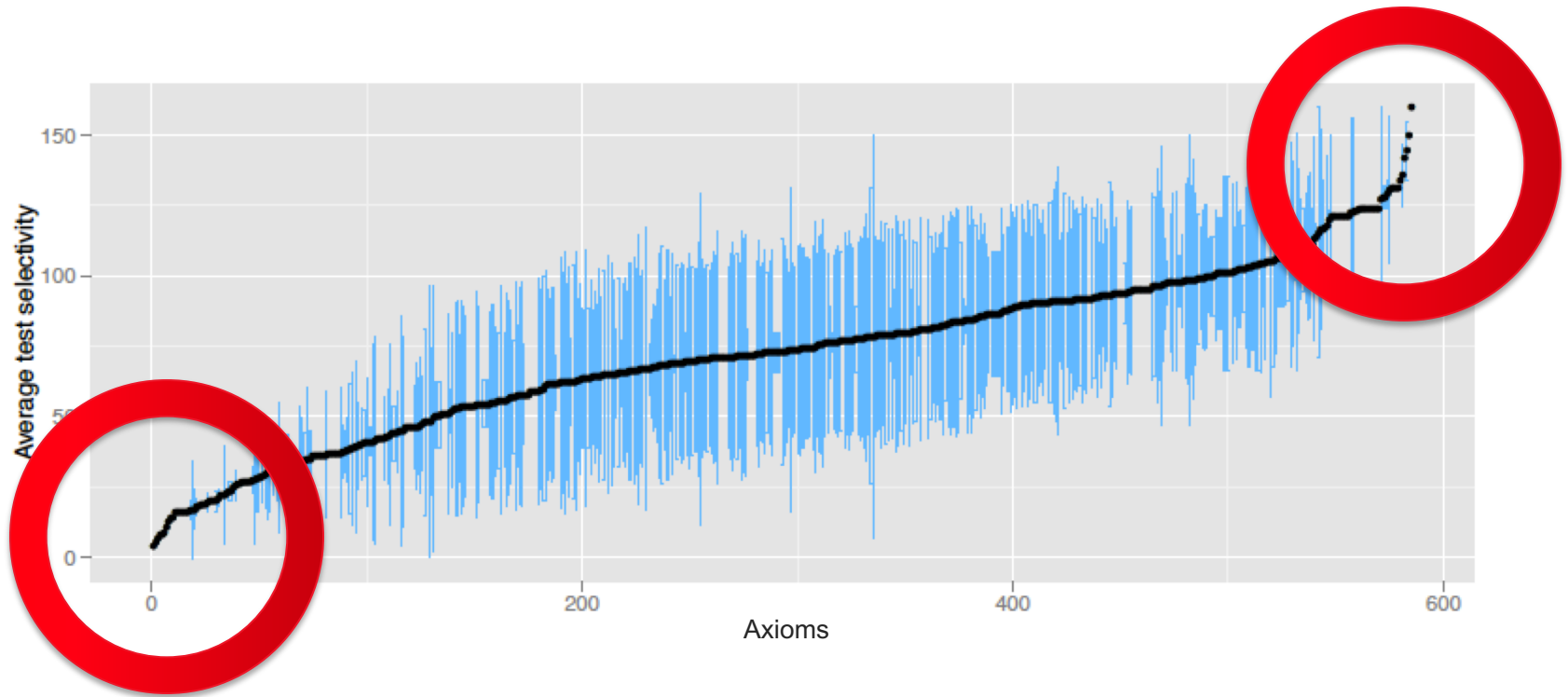
# Clustering Results



→ Problem understanding!

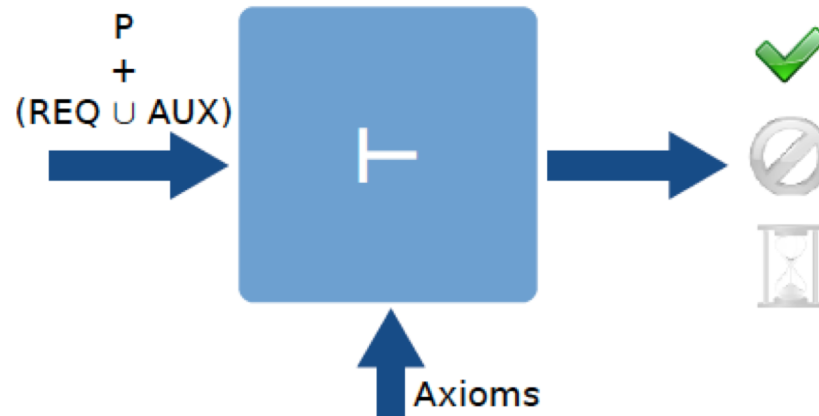


# Test Case Selectivity



Only specific test cases, or test cases with broad coverage for an axiom may not be sufficient.

# Completeness Coverage



Definition (Completeness Coverage, TAP 2013)

A test case  $P + (REQ \cup AUX)$  covers the set of *Axioms* if

- $Axioms \vdash P + (REQ \cup AUX)$
- and this does not hold for  $Axioms' \subsetneq Axioms$

Note: covered set *Axioms* is not uniquely defined by the test case



# Computing Completeness Coverage

Given: set of axioms  $Ax$  and completeness test case  $T$

Result: completeness coverage by  $T$

1. Run tool on  $T$ , record resource consumptions (to get upper limit for the subsequent runs).
  2. If available, analyse proof artifacts to restrict the next step to a subset of  $Ax$ .
  3. Remove stepwise from  $Ax$  and check if proof is still valid.
- [repeat until a fix-point is reached]

Computing coverage for most test cases takes from a few minutes to several hours.